DS 4400

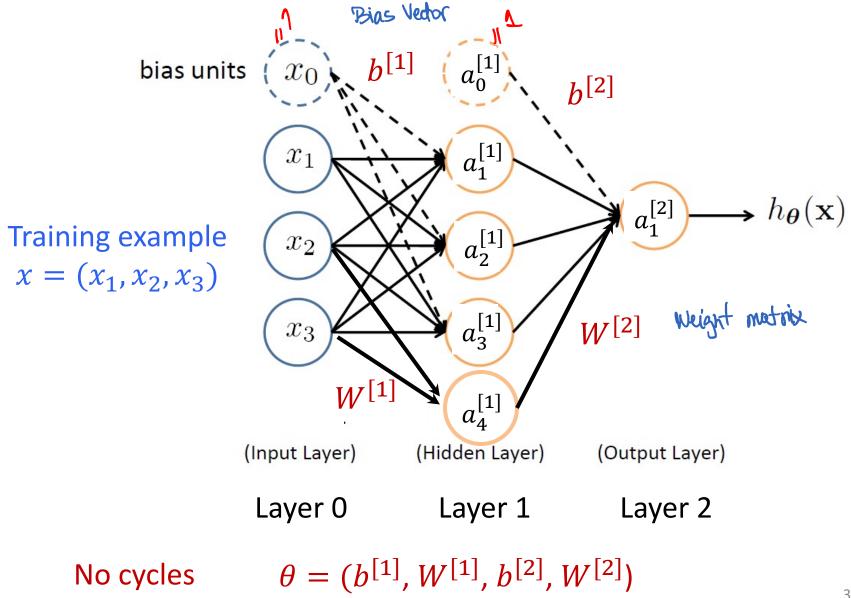
Machine Learning and Data Mining I Spring 2021

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Outline

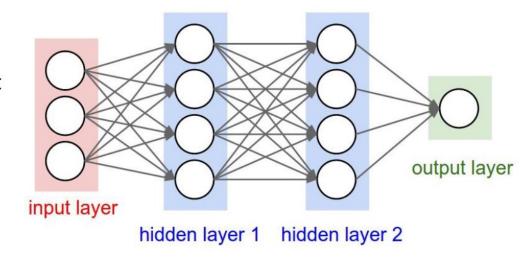
- Keras tutorial on feed-forward neural networks
- Convolutional neural networks
 - Convolution operation
 - Max pooling
 - Estimating parameters
- Architectures for convolutional networks
- Lab in Keras on convolutional networks

Feed-Forward Neural Network



Forward Propagation

- The input neurons first receive the data features of the object. After processing the data, they send their output to the first hidden layer.
- The hidden layer processes this output and sends the results to the next hidden layer.
- This continues until the data reaches the final output layer, where the output value determines the object's classification.
- This entire process is known as Forward Propagation, or Forward prop.

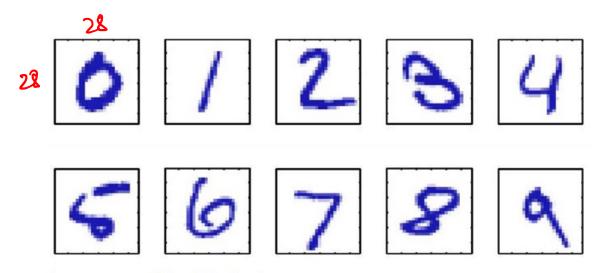


x — Prediction

Multi-class classification

MULTI-LAYER PERCEPTRON (MLP) \rightarrow P(y = 0 | x) ightharpoonup P(y = 1 | x) \rightarrow P(y = 2 | x) K CLASES Softmax Input Features I Features II classifier

MNIST: Handwritten digit recognition



Images are 28 x 28 pixels

Represent input image as a vector $\mathbf{x} \in \mathbb{R}^{784}$ Learn a classifier $f(\mathbf{x})$ such that, $f: \mathbf{x} \to \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$

> Predict the digit Multi-class classifier

Lab — Feed Forward NN

```
import time
import numpy as np
#!pip install tensorflow
#!pip install keras

from keras.utils import np_utils
import keras.callbacks as cb
from keras.models import Sequential
from keras.layers.core import Dense, Dropout, Activation
from keras.optimizers import RMSprop
from keras.datasets import mnist

import matplotlib
import matplotlib.pyplot as plt
```

Import modules

```
def load_data():
    print("Loading data")
    (X_train, y_train), (X_test, y_test) = mnist.load_data()

X_train = X_train.astype('float32')

X_test = X_test.astype('float32')

# Normalize
    X_train /= 255
    X_test /= 255

y_train = np_utils.to_categorical(y_train, 10)
    y_test = np_utils.to_categorical(y_test, 10)

X_train = np.reshape(X_train, (60000, 784))
    X_test = np.reshape(X_test, (10000, 784))

print("Data loaded")
```

return [X train, X test, y train, y test]

Load MNIST data Processing

Vector representation

Neural Network Architecture

```
def init model1():
    start time = time.time()
    print("Compiling Model")
                                                                10 hidden units
    model = Sequential()
   model.add(Dense(10, input dim=784))
                                                                ReLU activation
   model.add(Activation('relu'))
    model.add(Dense(10))
                                                                 Output Layer
    model.add(Activation('softmax'))
                                                                 Softmax activation
    rms = RMSprop()
    model.compile(loss='categorical crossentropy', optimizer=rms, metrics=['accuracy'])
    print("Model finished "+format(time.time() - start time)
    return model
                                                        Optimizer
                            Loss function
```

Feed-Forward Neural Network Architecture

- 1 Hidden Layer ("Dense" or Fully Connected)
- 10 neurons
- Output layer uses softmax activation

Number of Parameters

```
model1.summary()
Model: "sequential 6"
Layer (type)
                              Output Shape
                                                         Param #
dense 16 (Dense)
                              (None, 10)
                                                         7850
activation 16 (Activation)
                              (None, 10)
                                                         0
dense 17 (Dense)
                              (None, 10)
                                                         110
activation 17 (Activation)
                              (None, 10)
                                                         0
Total params: 7,960
Trainable params: 7,960
Non-trainable params: 0
```

Train and evaluate

```
def run network(data=None, model=None, epochs=20, batch=256):
   try:
        start time = time.time()
        if data is None:
            X train, X test, y train, y test = load data()
        else:
            X train, X test, y train, y test = data
       print("Training model")
        history = model.fit(X train, y train, epochs=epochs, batch size=batch,
                  validation data=(X test, y test), verbose=2)
       print("Training duration:"+format(time.time() - start time))
        score = model.evaluate(X test, y test, batch size=16)
        print("\nNetwork's test loss and accuracy:"+format(score))
        return history
   except KeyboardInterrupt:
        print("KeyboardInterrupt")
        return history
```

Training/testing results

Changing Number of Neurons

```
def init_model2():
    start_time = time.time()

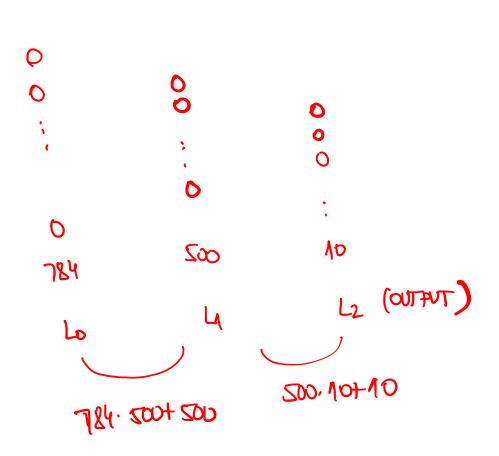
    print("Compiling Model")
    model = Sequential()
    model.add(Dense(500, input_dim=784))
    model.add(Activation('relu'))

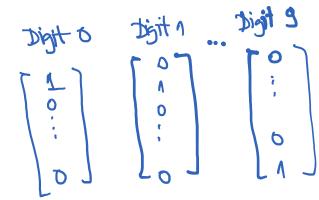
    model.add(Dense(10))
    model.add(Activation('softmax'))

    rms = RMSprop()
    model.compile(loss='categorical_crossentropy', optimizer=rms, metrics=['accuracy'])

    print("Model finished "+format(time.time() - start_time))
    return model
```

Number of Parameters





Number of Parameters

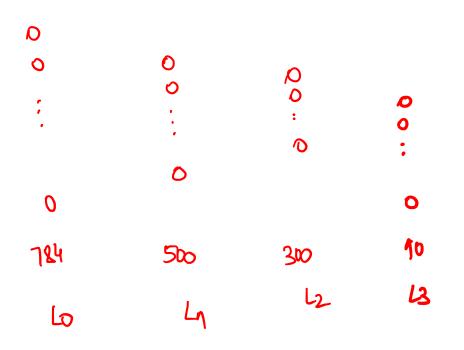
```
model2.summary()
Model: "sequential 9"
                              Output Shape
                                                         Param #
Layer (type)
dense 22 (Dense)
                              (None, 500)
                                                         392500
activation 22 (Activation)
                              (None, 500)
dense 23 (Dense)
                                                         5010
                              (None, 10)
activation 23 (Activation)
                              (None, 10)
Total params: 397,510
Trainable params: 397,510
Non-trainable params: 0
```

Two Layers

```
def init model4():
   start time = time.time()
   print("Compiling Model")
   model = Sequential()
   model.add(Dense(500, input dim=784))
   model.add(Activation('relu'))
   model.add(Dropout(0.4))
   model.add(Dense(300))
   model.add(Activation('relu'))
   model.add(Dropout(0.4))
   model.add(Dense(10))
   model.add(Activation('softmax'))
   rms = RMSprop()
   model.compile(loss='categorical crossentropy', optimizer=rms, metrics=['accuracy'])
   print("Model finished"+format(time.time() - start time))
   return model
```

..... 15

Number of Parameters



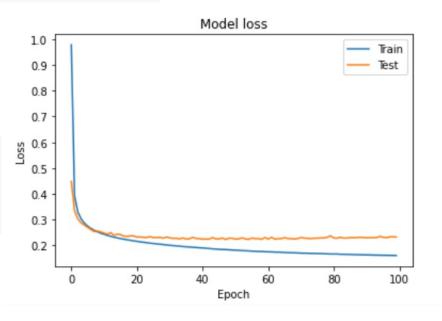
Model Parameters

model4.summary()			
Model: "sequential_11"			
Layer (type)	Output	Shape	Param #
dense_26 (Dense)	(None,	500)	ما 392500 سرحما
activation_26 (Activation)	(None,	500)	0
dropout_9 (Dropout)	(None,	500)	0
dense_27 (Dense)	(None,	300)	150300 4->12
activation_27 (Activation)	(None,	300)	0
dropout_10 (Dropout)	(None,	300)	0
dense_28 (Dense)	(None,	10)	3010 2-313
activation_28 (Activation)	(None,	10)	0
Total params: 545,810 Trainable params: 545,810 Non-trainable params: 0			

Monitor Loss

```
def plot_losses(hist):
    plt.plot(hist.history['loss'])
    plt.plot(hist.history['val_loss'])
    plt.title('Model loss')
    plt.ylabel('Loss')
    plt.xlabel('Epoch')
    plt.legend(['Train', 'Test'], loc='upper right')
    plt.show()
```

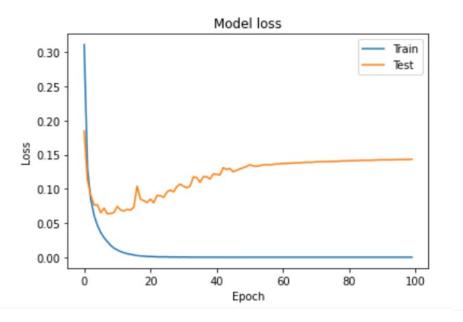
```
model1 = init_model1()
history1 = run_network(model = model1, epochs=100)
plot_losses(history1)
```

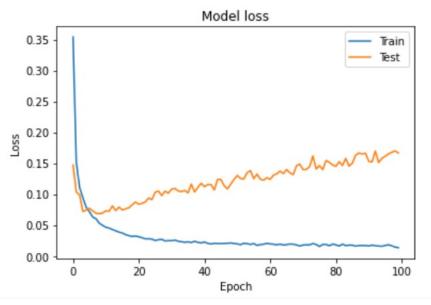


Loss

```
model2 = init_model2()
history2 = run_network(model = model2, epochs=100)
plot_losses(history2)
```

```
model4 = init_model4()
history4 = run_network(model = model4, epochs=100)
plot_losses(history4)
```





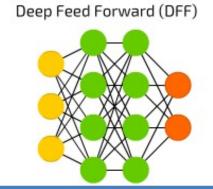
Review FFNN

- Feed-Forward Neural Networks are the common neural networks architectures
 - Fully connected networks are called Multi-Layer Perceptron
- Input, output, and hidden layers
 - Linear matrix operations followed by non-linear activations at every layer
- Activations:
 - ReLU, tanh, etc., for hidden layers
 - Sigmoid (binary classification) and softmax (for multiclass classification) at last layer
- Forward propagation: process of evaluating input through the network

Neural Network Architectures

Feed-Forward Networks

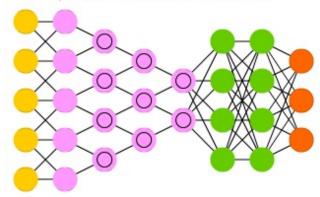
 Neurons from each layer connect to neurons from next layer



Convolutional Networks

- Includes convolution layer for feature reduction
- Learns hierarchical representations

Deep Convolutional Network (DCN)



Recurrent Networks

- Keep hidden state
- Have cycles in computational graph

Recurrent Neural Network (RNN)

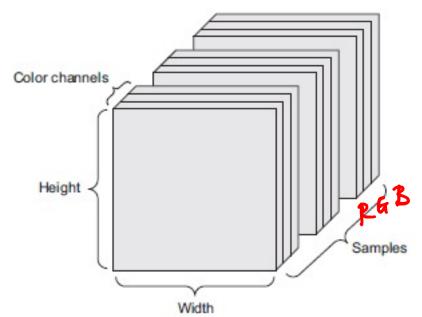


Convolutional Nets

- Particular type of Feed-Forward Neural Nets
 - Invented by [LeCun 89]
- Applicable to data with natural grid topology
 - Time series
 - Images
- Use convolutions on at least one layer
 - Convolution is a linear operation that uses local information
 - Also use pooling operation
 - Used for dimensionality reduction and learning hierarchical feature representations

Image Representation

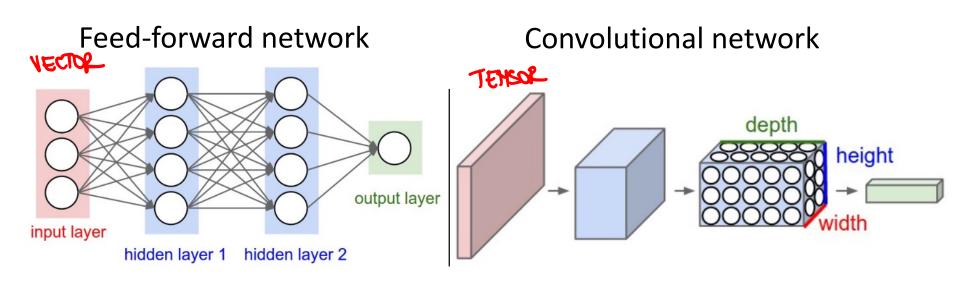
- Image is 3D "tensor": height, width, color channel (RGB)
- Black-and-white images are 2D matrices: height, width
 - Each value is pixel intensity

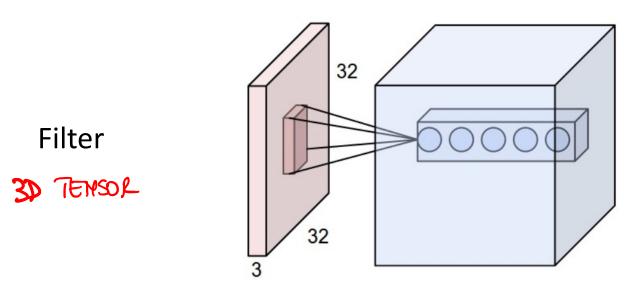


Computer vision principles

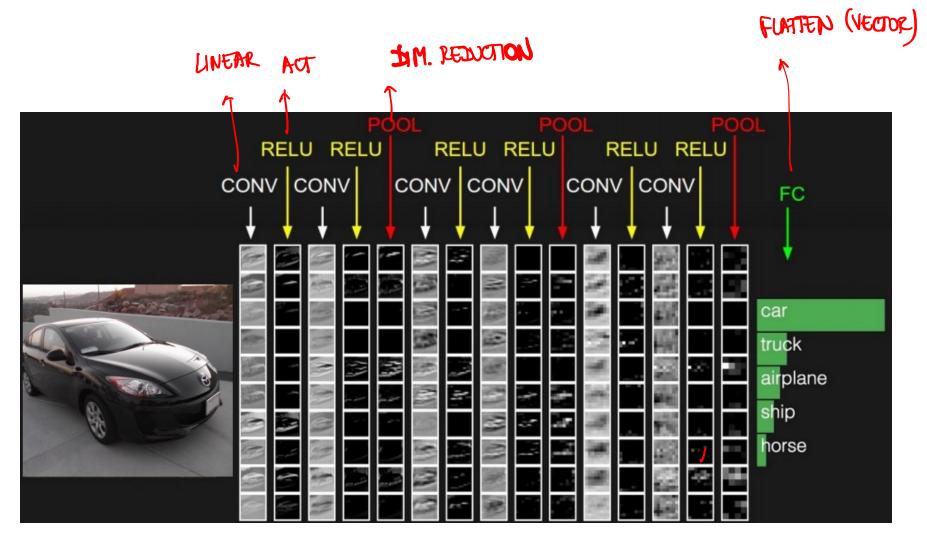
- Task: image classification (object identification)
- Translation invariance
 - Classification should work if object appears in different locations in the image => All image regions are treated the same
- Locality
 - Focus on local regions for object detection => computation should be local
- Mathematical operation: Convolution

Convolutional Neural Networks





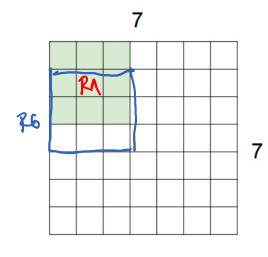
Convolutional Nets



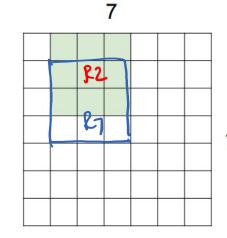
Convolutions 220

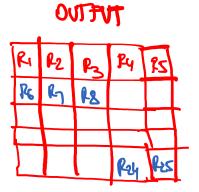


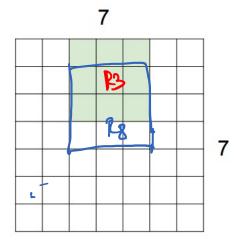
A closer look at spatial dimensions:

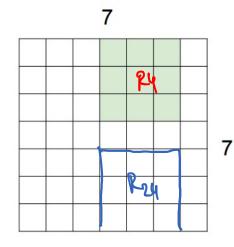


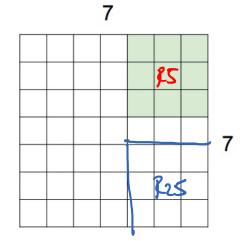
7x7 input (spatially) assume 3x3 filter



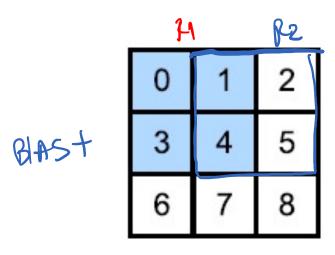


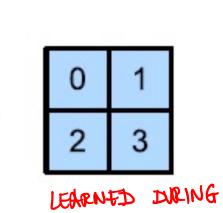






Example





Input

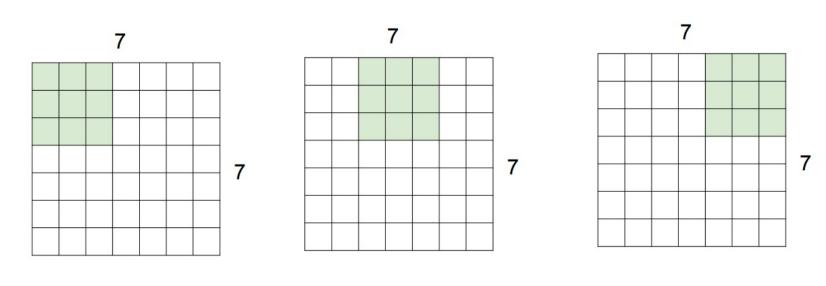
Filter

TRAINING

Output

Convolutions with stride

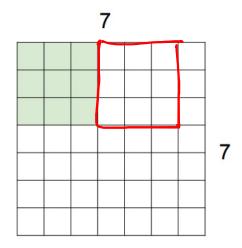
7x7 input (spatially) assume 3x3 filter applied with stride 2



OUTPUT: 3x3

Convolutions with stride

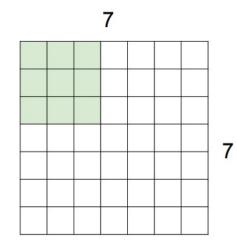
7x7 input (spatially) assume 3x3 filter applied with stride 3?



N F N

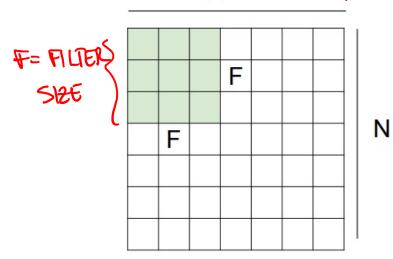
Convolutions with stride

7x7 input (spatially) assume 3x3 filter applied with stride 3?



doesn't fit! cannot apply 3x3 filter on 7x7 input with stride 3.

N = INPUT SHEE



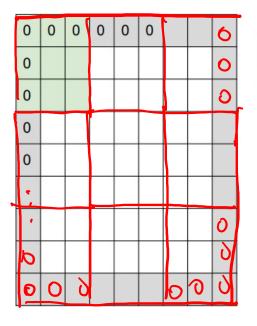
IF N-F NOT DIVISIBLE BY STUDE

ADD FADDING

Output size: (N - F) / stride + 1

Padding

In practice: Common to zero pad the border



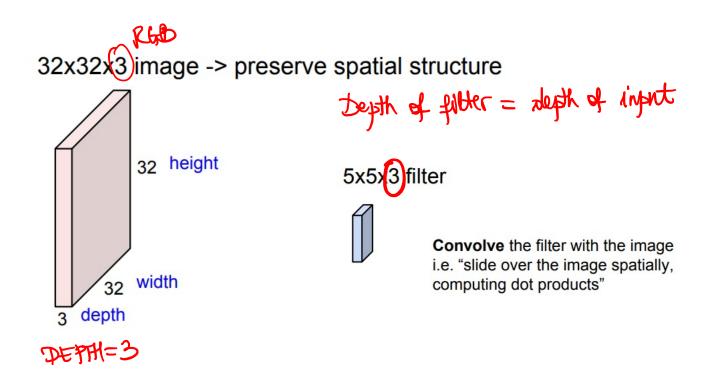
```
e.g. input 7x7

3x3 filter, applied with stride 3

pad with 1 pixel border => what is the output?
```

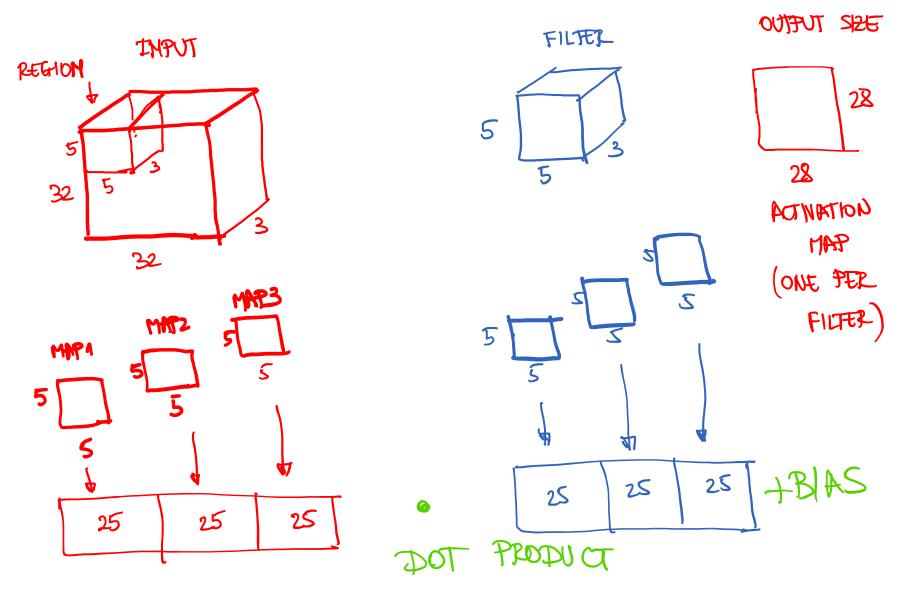
```
(recall:)
(N - F) / stride + 1
```

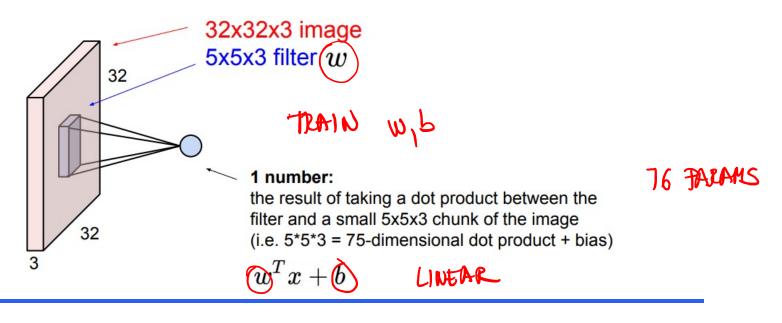


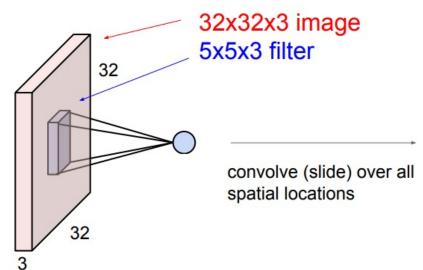


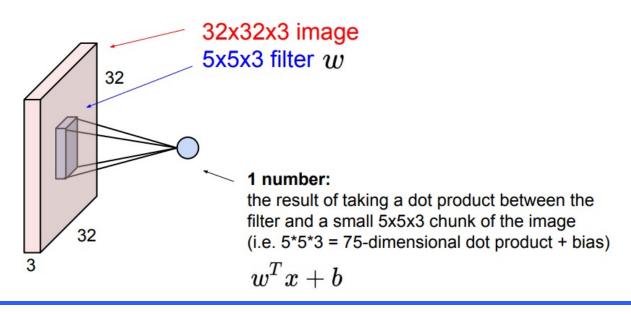
- Depth of filter always depth of input
- Computation is based only on local information

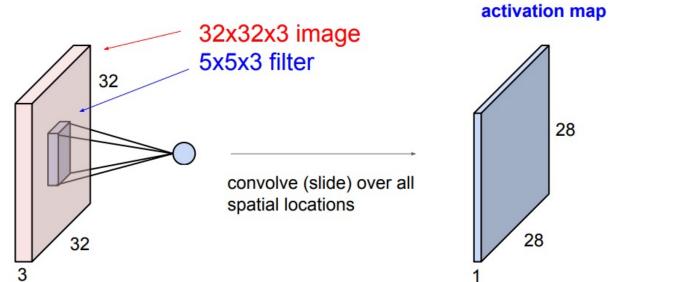
Convolution Operation

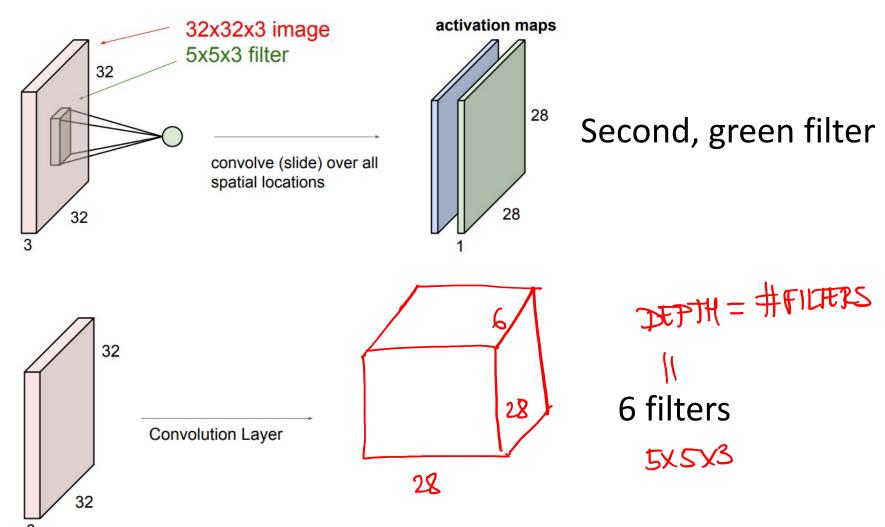


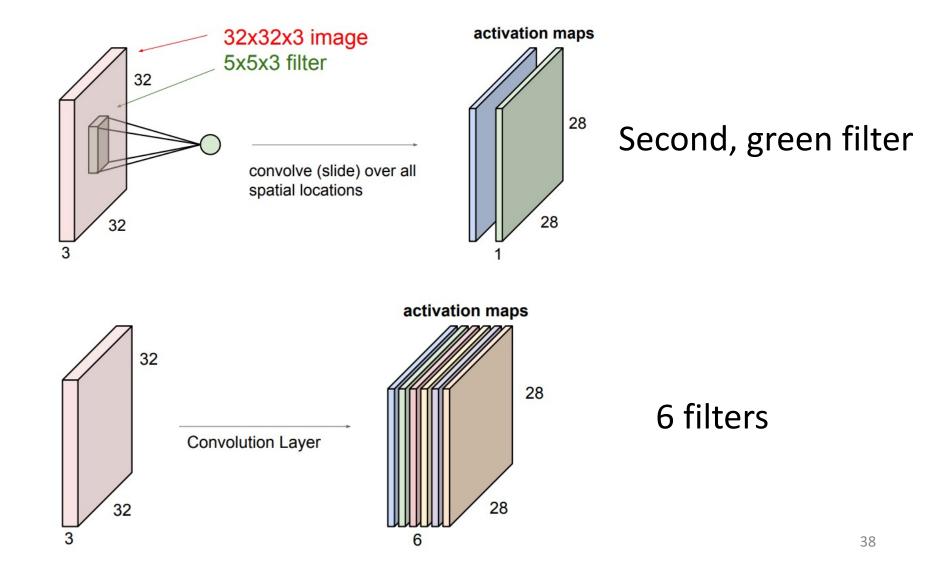










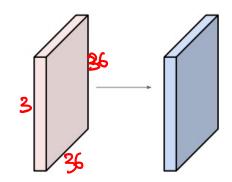


Examples

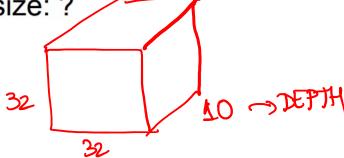
Examples time:

Input volume 36x36x3

10 5x5x3 filters with stride 1, pad 2



Output volume size: ?



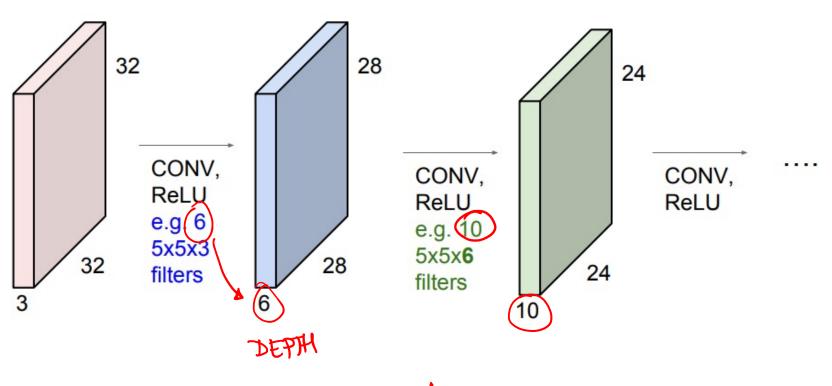
Number of parameters in this layer?

1 FILTER: 5X5X3+1=76

10 FIUERS: 760

Convolutional Nets

Preview: ConvNet is a sequence of Convolution Layers, interspersed with activation functions



Convolution layer: Takeaways

- Convolution is a linear operation
 - Reduces parameter space of Feed-Forward Neural Network considerably
 - Capture locality of pixels in images
 - Smaller filters need less parameters
 - Multiple filters in each layer (computation can be done in parallel)
- Convolutions are followed by activation functions
 - Typically ReLU

Acknowledgements

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 - Andrew Moore
 - Yann LeCun
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